

Name: Key Date: \_\_\_\_\_ Period: \_\_\_\_\_ Score: \_\_\_\_\_

**Intro to Calculus**  
**Chapter 3 PRACTICE Test (3.4 - 3.6)**  
You must show work to receive full credit!

1. What is the instantaneous rate of change at  $x = 3$  of the function  $f$  given by  $f(x) = \frac{x-3}{2x+5}$  ?

$$f'(x) = \frac{(2x+5)(1) - (x-3)(2)}{(2x+5)^2} = \frac{2x+5-2x-6}{(2x+5)^2} = \frac{-1}{(2x+5)^2}$$

$$f'(3) = \frac{-1}{(6+5)^2} = \frac{-1}{121}$$

2. If  $f(x) = -2x^3 + 2x + \frac{1}{x^2}$ , then  $f'(-1) = -6(-1)^2 + 2 - 2(-1)^{-3} = -6 + 2 + 2 = -2$

$$f(x) = -2x^3 + 2x + x^{-2}$$

$$f'(x) = -6x^2 + 2 - 2x^{-3}$$

$$f'(-1) = -2$$

3. A particle starts at time  $t = 0$  and moves along the  $x$ -axis so that its position at any time  $t \geq 0$  seconds is given by  $x(t) = (t+2)^2(t-3)$  meters.

(a) Write  $x(t)$  in standard form rather than factored form. (This will make the next steps much easier ☺)

$$x(t) = (t^2 + 4t + 4)(t-3)$$

$$t^3 + 4t^2 + 4t$$

$$+ \frac{-3t^2 - 12t - 12}{\hline}$$

$$x(t) = t^3 + t^2 - 8t - 12$$

(b) Find the velocity of the particle at any time  $t \geq 0$ .

$$v(t) = 3t^2 + 2t - 8$$

(c) Find the acceleration at  $t = 4$  seconds.

$$a(t) = 6t + 2$$

$$a(4) = 6(4) + 2 = 26 \text{ units/sec}^2$$

~~(d) Find the value of  $t$  when the particle is moving and the acceleration is zero.~~

$$6t + 2 = 0$$

## Intro to Calculus

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4. Which of the following is an equation of the line tangent to the graph of  $f(x) = 12x^3 - 4x$  at the point

where  $f'(x) = 12$  and  $x$  is positive?

$$y = 12x - \frac{64}{9}$$

$$8/9 = 12(2/3) + b$$

$$8/9 = 8 + b$$

$$-\frac{64}{9} = b$$

$$f'(x) = 36x^2 - 4$$

$$12 = 36x^2 - 4$$

$$16 = 36x^2$$

$$x^2 = \frac{16}{36} = \frac{4}{9} \quad x = \pm \frac{2}{3}$$

$$f(2/3) = 12(2/3)^3 - 4(2/3)$$

$$x = 2/3$$

$$f'(2/3) = 8/9$$

5. If  $f(x) = \sqrt{3x^2}$ , then  $f'(1) = \sqrt{3}$

$$f'(x) = \frac{1}{2} (3x^2)^{-1/2} (6x) \quad f'(1) = \frac{1}{2} (3(1)^2)^{-1/2} (6(1)) = 3(3)^{-1/2} = \frac{3}{\sqrt{3}} = \sqrt{3}$$

6. A particle moves along a straight line with velocity given by  $v(t) = (3t^2 - 1)^4$  at time  $t \geq 0$ . What is the acceleration of the particle at time  $t = 3$ ?

$$a(t) = 4(3t^2 - 1)^3 (6t)$$

$$a(3) = 4(3(3)^2 - 1)^3 (6(3))$$

$$a(3) = 1,265,472 \quad \leftarrow \text{That's fast!}$$

7. If  $f(x) = (2x)(x^2 - 1)^4$ , then  $f'(x) =$

$$f'(x) = 2(x^2 - 1)^4 + 2x(4(x^2 - 1)^3(2x))$$

$$f'(x) = 2(x^2 - 1)^4 + 16x^2(x^2 - 1)^3$$

8. If  $f(x) = \sin(3x)$ , then  $f'\left(\frac{\pi}{2}\right) =$

$$f'(x) = 3\cos(3x)$$

$$f'\left(\frac{\pi}{2}\right) = 3\cos\left(\frac{3\pi}{2}\right) = 3(0) = 0$$

9. What is the slope of the line tangent to the curve  $y = \sec(4x)$  at the point at which  $x = \frac{\pi}{4}$ ?

$$y' = 4\sec(4x)\tan(4x)$$

$$y'\left(\frac{\pi}{4}\right) = 4\sec(\pi)\tan(\pi)$$

$$= 4(-1)(0)$$

$$y'\left(\frac{\pi}{4}\right) = 0$$